

If the annual rate of inflation averages 5% over the next ten years, the approximate cost of C of goods or services during any year in that decade is:

$$C(t) = P(1.05)^t$$

where t is the time in years and P is the present cost.

a) if the price of an oil change for your car is presently \$24.95, estimate the price 10 years from now?

$$C(10) = 24.95(1.05)^{10}$$

$$C(10) = 40.64$$

b) Find the rate of change of C with respect to t when t=1 and t=8

$$C(t) = P(1.05)^t$$

$$\frac{dC}{dt} = P \cdot \ln(1.05) \cdot 1.05^t$$

$$a^u = \ln(a) a^u \frac{du}{dt}$$

$$C'(t) = P \ln(1.05) 1.05^t$$

t=1

$$C'(1) = 0.05P$$

t=8

$$C'(8) = 0.07P$$

After  $t$  years, the value of a car purchased for \$20,000 is:

$$V(t) = 20,000 \left(\frac{3}{4}\right)^t$$

a) Determine the value of the car 2 years after it was purchased.

$$V(2) = 20,000 \left(\frac{3}{4}\right)^2 = 11250$$

b) Find the rate of change of  $V$  with the respect to  $t$  when  $t=1$  and  $t=4$ .

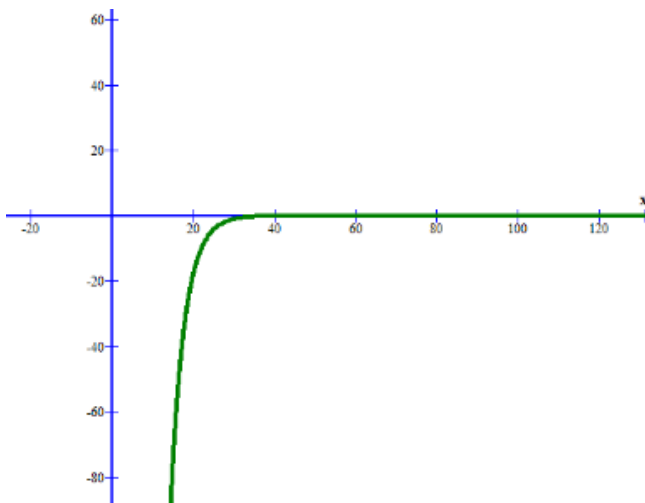
$$V(t) = 20,000 \left(\frac{3}{4}\right)^t$$

$$(20,000) \ln \frac{3}{4} \cdot \frac{3}{4}^t \cdot 1$$

$$V'(1) = -4315.231$$

$$V'(4) = -67.425$$

c) use a graphing utility to graph  $v'(t)$  and determine the horizontal asymptote of  $V'(t)$ . Interpret its meaning



asymptote at  $x=0$ .

this means there is a point when the car stops losing value, and maintains its value. This value is probably very small, but not zero.

Assume that you can earn 6% on an investment compounded daily. Which of the following options would yield the greatest balance in 8 years?

Compounding n times a year:  $A = P\left(1 + \frac{r}{n}\right)^{nt}$

a) 20,000 now  $A = 20,000 \left(1 + \frac{.06}{365}\right)^{365 \cdot 8}$   
 $A = 32,320.21$

b) 30,000 in 8 years

it didn't have anytime to gain interest

$A = 30,000$

c) \$8000 now and \$20,000 in 4 years  $A = P\left(1 + \frac{r}{n}\right)^{nt}$

$8000 \left(1 + \frac{.06}{365}\right)^{365 \cdot 8}$   
 2920  
 1460  
 2928.085  
 25,424.481  
 37,852.566

$12928.08 + 25424.48$   
 $38,352.56$