

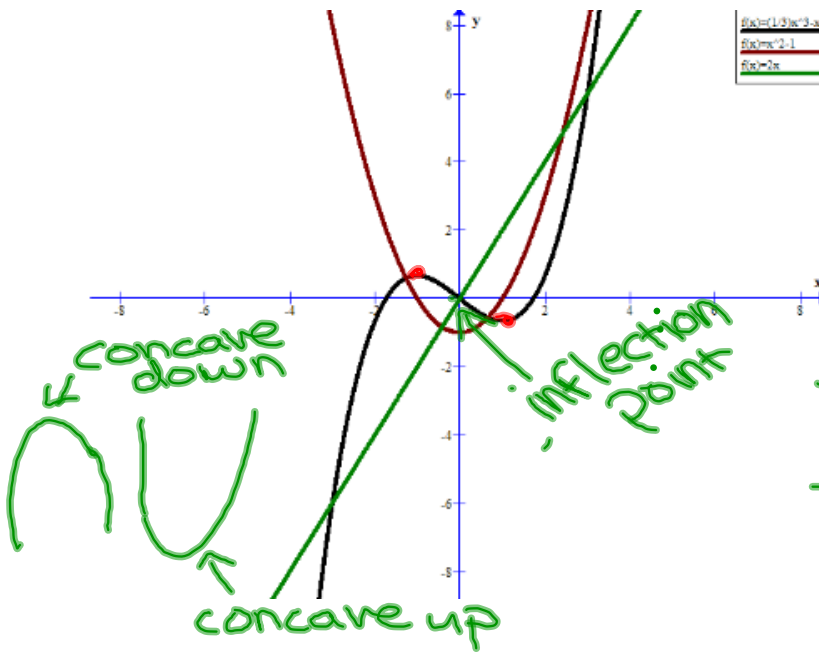
$$f(x) = \frac{1}{3}x^3 - x$$

$$f'(x) = x^2 - 1$$

$$f''(x) = 2x$$

$$f'(x) = 0: \text{mins, max}$$

$$f' > 0 = \text{increasing}$$



$f'(x) = 0$  : mins, max  
 $f'(x) > 0$  : increasing  
 $f'(x) < 0$  : decreasing

$f''(x) = 0$  : inflection point  
 $f''(x) < 0$  : concave down  
 $f''(x) > 0$  : concave up

## Second derivative rule

given  $f'(c) = 0$

$f''(c) > 0$  : maximum

$f''(c) < 0$  : minimum

extrema on concave down

 is a maximum