

$$(xy)^3 - y = x$$

$$x^3 y^3 - y = x$$

$$x^3 \cdot 3y^2 \frac{dy}{dx} + 3x^2 y^3 - \frac{dy}{dx} = 1$$

$$3x^3 y^2 \frac{dy}{dx} - \frac{dy}{dx} = 1 - 3x^2 y^3$$

$$\frac{dy}{dx} (3x^3 y^2 - 1) = 1 - 3x^2 y^3$$

$$\frac{dy}{dx} = \frac{1 - 3x^2 y^3}{3x^3 y^2 - 1}$$

$$\sin \sqrt{x} + \sqrt{\sin x}$$

$$\cos \sqrt{x} \cdot \frac{1}{2} x^{-1/2} + \frac{1}{2} (\sin x)^{-1/2} \cdot \cos x$$

$$\frac{\sqrt{x}}{\sqrt{x}} \frac{\cos \sqrt{x}}{2\sqrt{x}} + \frac{\cos x}{2\sqrt{\sin x}} \cdot \frac{\sqrt{\sin x}}{\sqrt{\sin x}}$$

$$\frac{\sqrt{x} \cos \sqrt{x}}{2x} + \frac{\cos x \sqrt{\sin x}}{2\sin x}$$

$$\tan(x+y) = x$$

$$\frac{\sin(x+y)}{\cos(x+y)} = x$$

$$\sin(x+y) = x \cos(x+y)$$

$$\cos(x+y) \left(1 + \frac{dy}{dx}\right) = 1 \cdot \cos(x+y) - x \cdot \sin(x+y) \left(1 + \frac{dy}{dx}\right)$$

$$\begin{aligned} \cos(x+y) + \cos(x+y) \frac{dy}{dx} &= \cos(x+y) - x \sin(x+y) - x \sin(x+y) \frac{dy}{dx} \\ \cos(x+y) \frac{dy}{dx} + x \sin(x+y) \frac{dy}{dx} &= \cancel{\cos(x+y)} - \cancel{\cos(x+y)} - x \sin(x+y) \end{aligned}$$

$$\frac{dy}{dx} (\cos(x+y) + x \sin(x+y)) = -x \sin(x+y)$$

$$\frac{dy}{dx} = \frac{-x \sin(x+y)}{\cos(x+y) + x \sin(x+y)}$$