

$$\sum_{i=1}^n c = cn$$

$$\sum_{i=1}^n i = \frac{n(n+1)}{2}$$

$$\sum_{i=1}^n i^2 = \frac{n(n+1)(2n+1)}{6}$$

$$\sum_{i=1}^n i^3 = \frac{n^2(n+1)^2}{4}$$

$$\begin{aligned}
& \sum_{i=1}^n \frac{i+1}{n^2} \\
& \frac{1}{n^2} \left(\sum_{i=1}^n i + 1 \right) \\
& \frac{1}{n^2} \left(\sum_{i=1}^n i + \sum_{i=1}^n 1 \right) \\
& \frac{1}{n^2} \left(\frac{n(n+1)}{2} + n \right) \\
& \frac{1}{n^2} \left(\frac{n^2+n}{2} + \frac{2n}{2} \right) \\
& \frac{1}{n^2} \left(\frac{n^2+3n}{2} \right) \\
& \frac{n+3}{2n}
\end{aligned}$$

$$\lim_{x \rightarrow \infty} 3x = \infty$$

$$\lim_{x \rightarrow \infty} \frac{1}{x} = 0$$

$$\lim_{x \rightarrow \infty} \frac{1}{x^2} = 0$$

$$26. \frac{64}{n^3} \left(\frac{(n^2+n)(2n+1)}{6} \right)$$

$$\frac{64}{n^3} \left(\frac{2n^3 + 3n^2 + n}{6} \right)$$

$$\lim_{n \rightarrow \infty} \frac{64}{6} \left(2 + \frac{3}{n} + \frac{1}{n^2} \right)$$

$$\frac{18n^2 + 18n}{2n^2}$$

$$\frac{18}{n^2} \left(\frac{n(n+1)}{2} \right)$$

$$\frac{18(n^2+n)}{2n^2}$$

$$\frac{18n^2}{2n^2} + \frac{18n}{2n^2}$$

$$\frac{18}{2} = 9$$

$$\lim_{n \rightarrow \infty} \sum_{i=1}^n \left(\frac{i^2}{n^2} \right) \left(\frac{1}{n} \right)$$

$$\lim_{n \rightarrow \infty} \frac{1}{n^3} \sum_{i=1}^n i^2$$

$$\lim_{n \rightarrow \infty} \frac{1}{n^3} \frac{(n^2 + n)(2n + 1)}{6}$$

$$\lim_{n \rightarrow \infty} \frac{2n^3 + 3n^2 + n}{6n^3}$$

$$\lim_{n \rightarrow \infty} \frac{2}{6} + \frac{3}{6n} + \frac{1}{6n^2}$$

$$\frac{2}{6} = \frac{1}{3}$$